# From data to decision-making under conditions of uncertainty

August 26th to 28th, 2025



Multi-criteria decision-making methods in the context of imperfect information for the assessment and management of natural risks

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# Natural risks management and contexts of decision-making





#### Decision-making context: natural risks management

Rapid mass movements in mountains (avalanches, floods, rockfalls....)







... threaten people and infrastructures







We try to **get protected** against them with good decisions and actions





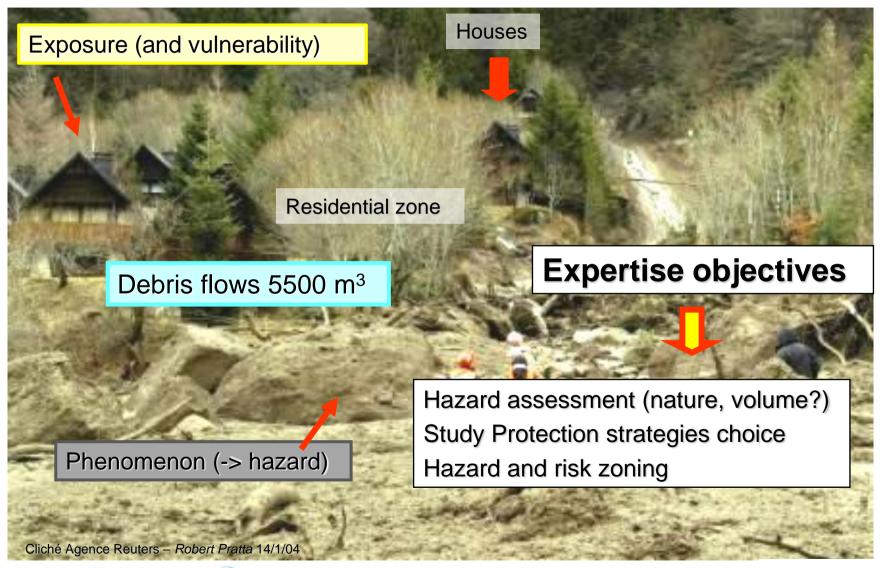




Jean-Marc Tacnet

#### Examples of challenging decisions associated to expertise process

#### Emergency zone evacuation (50 houses): Should we protect or destroy?



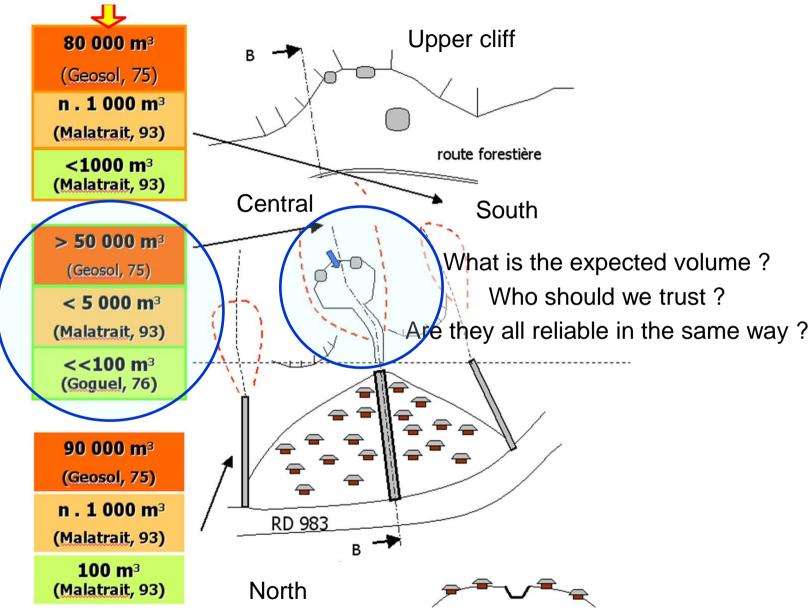








#### Landslide's **potential volume** estimated by **experts** ....





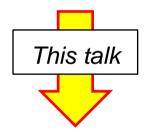






#### **Motivation**

- Risk management itself is a complex decision process (actors, time and spatial scales...)
- Information used to analyze risk is often imperfect (not only uncertain): how can we take a decision in this context? How can we be confident in the decision taken?



To introduce multicriteria decision-making methods (MCDM) and show some developments using (new) uncertainty theories for decisionmaking under information imperfection









#### **Outline**

Context and motivation

Information imperfection and some (useful) theories

Developments mixing MultiCriteria Decision-Making (MCDM) and information imperfection

Conclusion









# Information imperfection...

rather than (only) uncertainty

"Not everything that can be counted counts. Not everything that counts can be counted."

"Tout ce qui peut être compté ne compte pas forcément. Tout ce qui compte ne peut pas forcément être compté"

(Cameron, W.B., 1963) in "Informal Sociology: A Casual Introduction to Sociological Thinking"









#### Some situations (e.g.)...

- "The avalanche will follow this track, no this one ": Two (several) experts have different conclusions;
- "I am sure that the volume will be between 5000 and 10000 m<sup>3</sup>": the expert is **certain** but **imprecise**;
- "I am 75% confident in the fact that the volume will be between 5000 and 10000 m<sup>3</sup>": the expert is **uncertain** and **imprecise**:;
- "I just do not know what is the physical process (the expert may even not know that it exists)": the expert is lacking of information; information is missing;
- . "We will get 10mm rain today": Nature is uncertain (aleatory);
- . "1% chance that the cliff will collapse but we can investigate more precisely": an expert is uncertain (partial knowledge, epistemic)



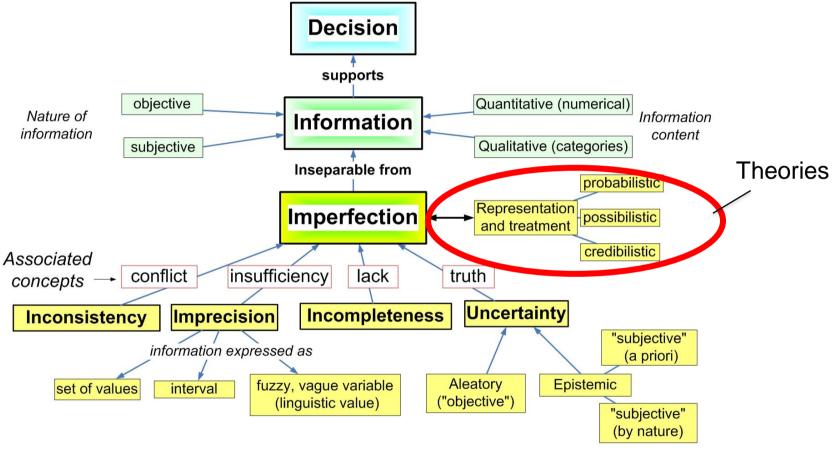






#### Uncertainty is not the only kind of information imperfection...

Probabilities are mostly used but different frameworks\* may have an interest



adapted from Smets, Dubois, Bosc, Bonissone, Tong...

(Tacnet, 2009)

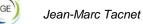
<sup>\*</sup> See also Konieczny, S. et Prade, H. (Eds.), 2020. L'intelligence artificielle, De quoi s'agit-il vraiment, Cepadues Editions, Toulouse, France.











# Fuzzy sets and possibility theories





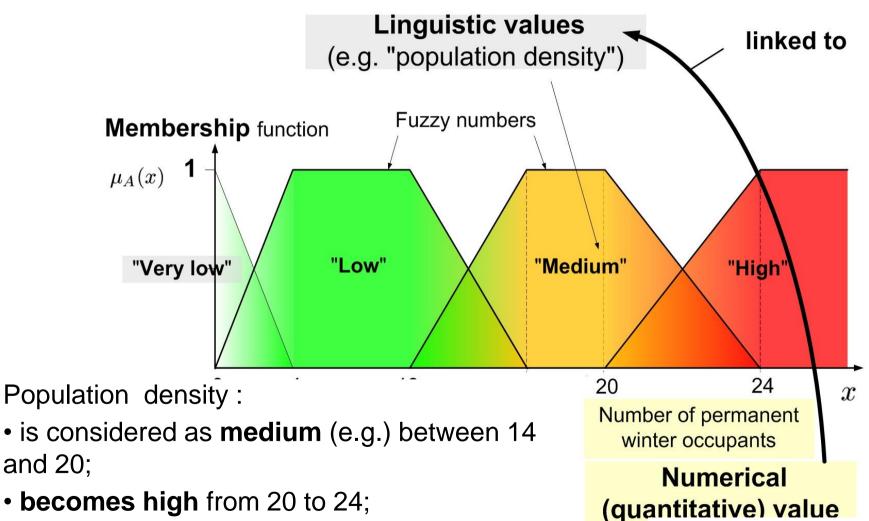






#### Fuzzy sets theory links numerical and linguistic values

(Zadeh, 1965)











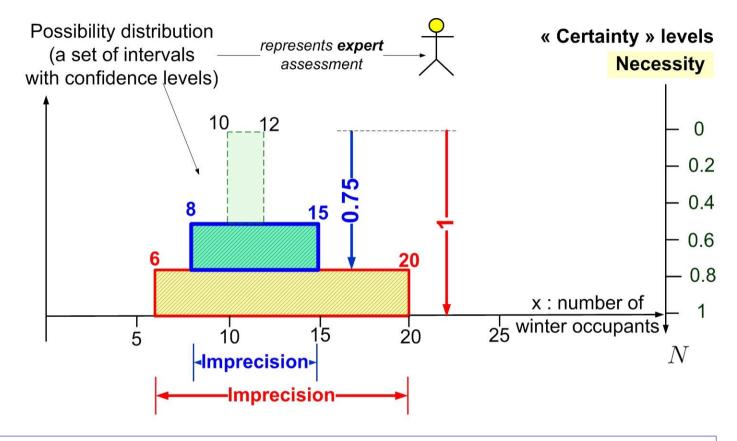
• becomes low from 14 to 10.



See (Tacnet et al., 2009, 2010)

#### Possibility theory (to represent both imprecision and uncertainty)

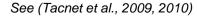
(Zadeh, 1978) (Dubois, 1988)



Evaluation of the **expert** is **imprecise**: he thinks that "Number of occupants is between 8 and 15"

The expert is **uncertain**: his certainty level for "Number of occupants is between 8 and 15" equals 0.75

The expert is still imprecise but certain that "Number of occupants is between 6 and 20"











## Belief function theory

... or how to go beyond probabilities

Belief = State of mind in which one thinks something to be true

#### Paradigm shift

Beliefs often are related with singular event or evidence, and are not necessarily related with statistical data and generic knowledge.









#### Belief function theory (Shafer, 1976)

The frame of discernment is a set of possible decisions, alternatives...

Decision hypothesis (e.g. "flooded", "not flooded")

Frame of discernment

$$\Theta = \{\theta_1, \theta_2\} \quad \theta_1 \quad \theta_2$$

Powerset  $\longrightarrow 2^{\Theta} = \{\emptyset, \theta_1, \theta_2, \theta_1 \cup \theta_2\}$ 

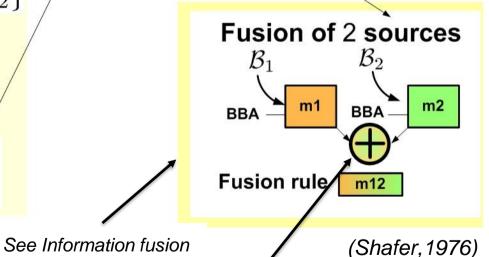
Basic Belief Assignment (BBA)

$$\begin{cases} m(.): 2^{\Theta} \to [0, 1] \\ m(\emptyset) = 0 \\ \sum_{\theta_i \in 2^{\Theta}} m(\theta_i) = 1 \end{cases}$$

$$m(\theta_1) + m(\theta_2) + \underbrace{m(\theta_1 \cup \theta_2)}_{uncertainty} = 1$$

e.g. "flooded" OR "not flooded" : uncertainty...

e.g. "expert x", "model y", "database z"



Many fusion rules exist







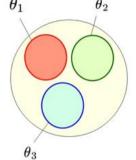


#### Belief functions' principles [Dempster 1967, Shafer 1976]

**Hypotheses** 

Frame of discernment (FoD)  $\Theta = \{\theta_i, i = 1, ..., n\}$  Power-set  $2^{\Theta} \triangleq \{X | X \subseteq \Theta\}$ 

Example



Impossibility partial ignorances full ignorance 
$$\downarrow \qquad \qquad \downarrow \qquad$$

**Basic belief assignment (BBA)**  $\mathfrak{m}(\cdot): 2^{\Theta} \mapsto [0,1]$  s.t.  $\mathfrak{m}(\emptyset) = 0$  and  $\sum \mathfrak{m}(A) = 1$ 

$$\mathfrak{m}(\cdot):2^{\Theta}\mapsto [0,1]$$

s.t. 
$$\mathfrak{m}(\emptyset) = 0$$

$$\sum_{A \in \mathcal{A}} \mathfrak{m}(A) = 1$$

$$Bel(A) \triangleq \sum_{B \in 2^{\Theta} \mid B \subseteq A} m(B) = Pl(\Theta) - Pl(\bar{A}) = 1 - Pl(\bar{A})$$

**Dearee** of support of A

$$Pl(A) \triangleq$$

$$\mathsf{n}(\mathsf{B}) = \mathsf{Bel}(\Theta) - \mathsf{Bel}(\bar{\mathsf{A}}) = 1 - \mathsf{Bel}(\bar{\mathsf{A}})_{\mathsf{cc}}^{\mathsf{D}}$$

Plausibility of A:  $Pl(A) \triangleq \sum_{m(B) = Bel(\Theta) - Bel(\bar{A}) = 1 - Bel(\bar{A}) = \frac{Degree \text{ of non}}{Contradiction \text{ of } A}$  $B \in 2^{\Theta} | B \cap A \neq \emptyset$ 

**Interpretation** 

$$0 \le Bel(A) \le P(A) \le Pl(A) \le 1$$

(subj.) unknown proba P(A)

The Uncertainty of unknown value of P(A) is PI(A)-BeI(A)



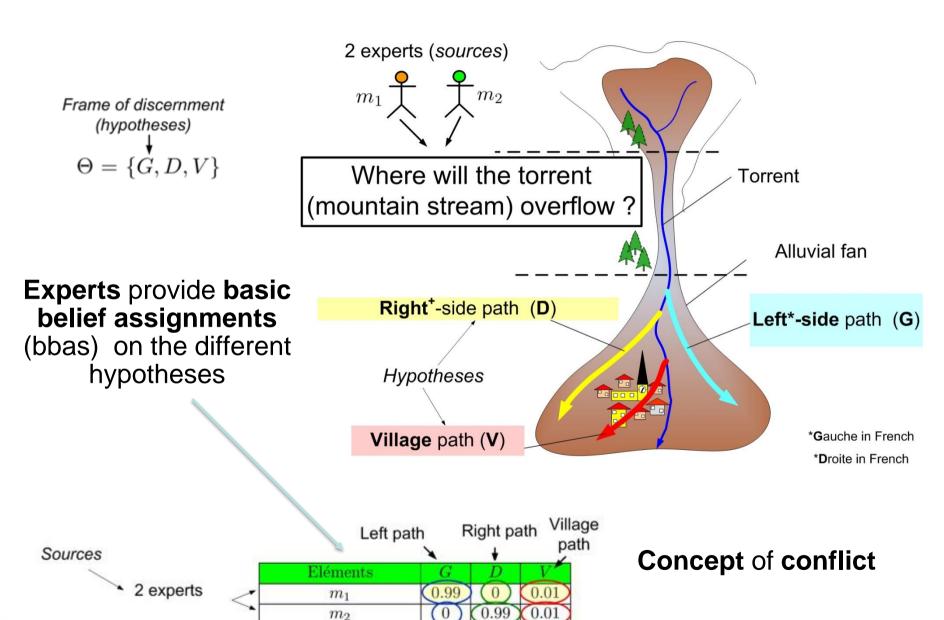






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#### **Belief function theory**





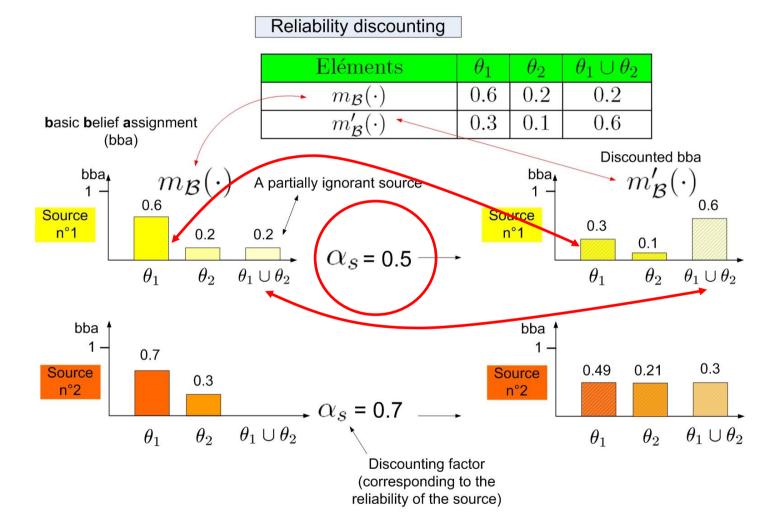








# Different information sources related to the same « truth » can be discounted according to their reliability











# Multicriteria decisionmaking principles and methods

Difference between total and partial agregation









#### 3 main categories of multicriteria decision-making problems

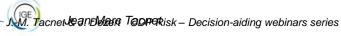
e.g. choosing the most effective, Decision problem ranking protection works according to their effectiveness... A : set of possible alternatives set of the most satisfactory  $A_1$ alternatives satisfactory  $A_2$ most satisfactory  $A_1$ alternatives alternatives existing categories  $A_k$ medium A\A<sup>+</sup>  $A_2$ satisfactory alternatives remaining alternatives most un- $A_k$ satisfactory alternatives An  $\alpha$ **Problematic Problematic Problematic** To choose To sort To rank

adapted from Schärlig (1985)

See (Tacnet,2009)









# Development of multicriteria decision-making methods ...considering information imperfection









Objective: to design **decision-aiding methods** in a context of **heterogeneous** and **imperfect information** provided by **more** or **less reliable sources**...



Use of **belief function theory** (and others theories) to improve **multicriteria decision-making** (MCDM) **methods** 

Principles of methods (several developped since 2009)...

ER-MCDA: replacing aggregation by a fusion process (Choice, Sorting...)

.... many others such as Soft Electre TRI: improving outranking method (Sorting) see references









#### **Developments**

## ER-MCDA\* methodology overview

\*Evidential Reasoning – MultiCriteria Decision Analysis

**ER-MCDA\*** associates (principles of) multicriteria decision analysis (AHP), fuzzy sets, possibility and belief function theories

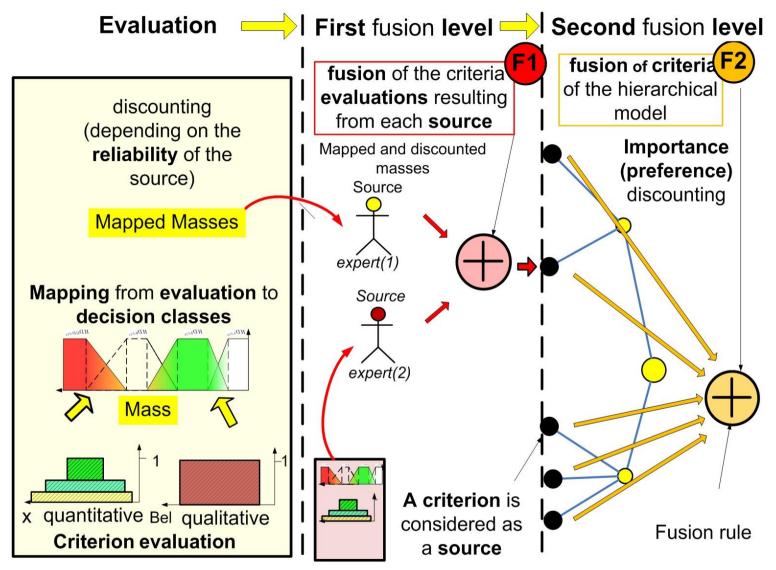
(Tacnet, 2009)











Analytic Hierarchy Process is (only) used to model the problem (aggregation is replaced by information fusion)

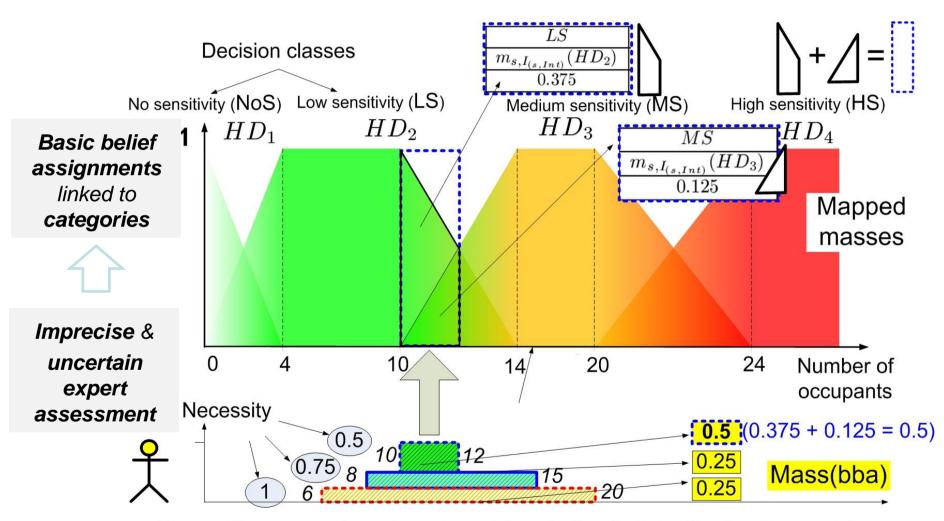








# A mapping process to link fuzzy sets, possibility and belief function theories



Source n°1 proposes an imprecise and uncertain evaluation of criterion "Number of occupants"

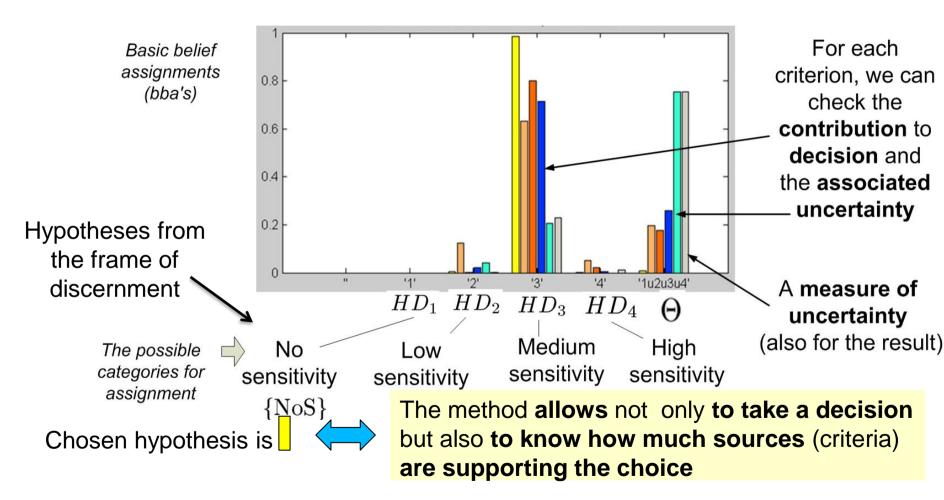








# The method provides not only a single choice but also proposes a "decision profile" that informs about information quality level











#### An application example

# Protection works'efficacy assessment

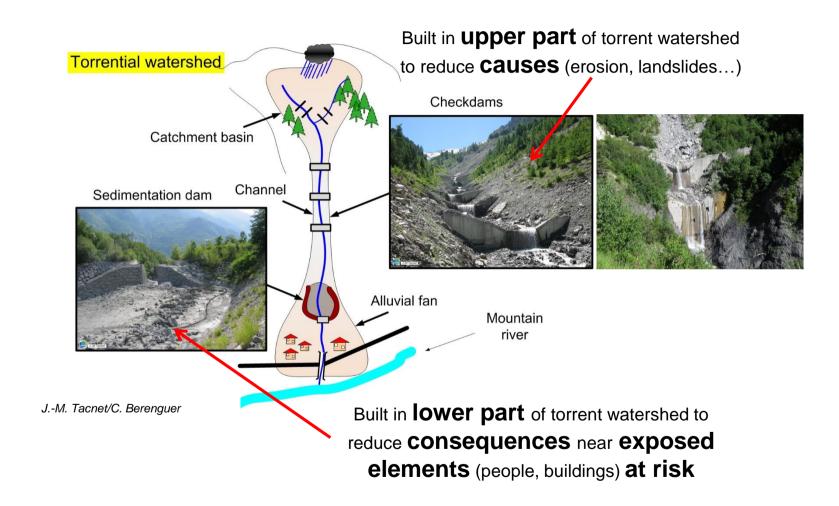








#### Structures are built to protect against, reduce natural risks



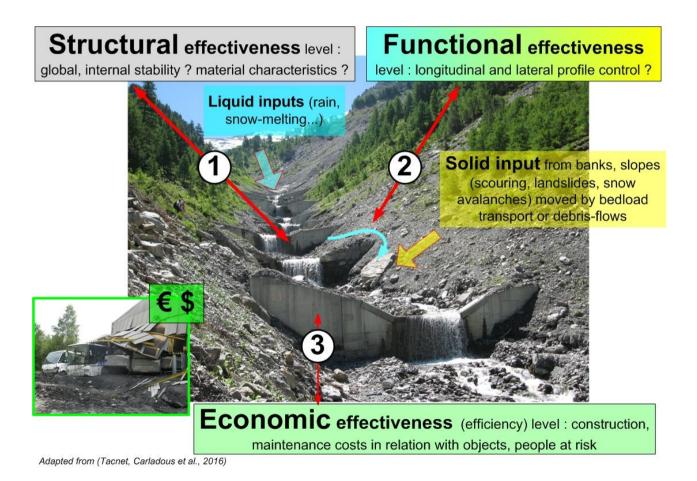








# Operational question: Are protection measures & strategies effective?











#### Decision to be taken: what is the checkdams' series efficacy?

#### 1. Alternatives A<sub>i</sub> to be assessed, ranked, stored

#### See Simon Carladous' PhD



Saint-Étienne

Nº d'ordre NNT : 2017LYSEM008

THESE de DOCTORAT DE L'UNIVERSITE DE LYON opérée au sein de

l'Ecole des Mines de Saint-Etienne

Ecole Doctorale № 488 Sciences, Ingénierie, Santé

Spécialité de doctorat : Sciences et génie de l'environnement

Soutenue publiquement le 05/04/2017, par : Simon Carladous

Approche intégrée d'aide à la décision basée sur la propagation de l'imperfection de l'information application à l'efficacité des mesures de protection torrentielle

Devant le jury composé de :

Breul, Pierre

Bossé, Eloi Grandjean, Gilles Directeur de recherche Dezert, Jean Maître de recherche

Batton-Hubert, Mireille Professeure

Docteur IGPEE Directeur de recherche

Irstea-UR ETGR ONF, Dép. RN

ONERA

IMT-Mines, St-Etienne

Univ. Blaise Pascal

Univ. Grenoble Alpes

Examinateur Directrice de thèse Co-encadrant de thèse

3 check dams' series

Function: stabilization

A,

28 check dams

25 check dams

A,



3 check dams



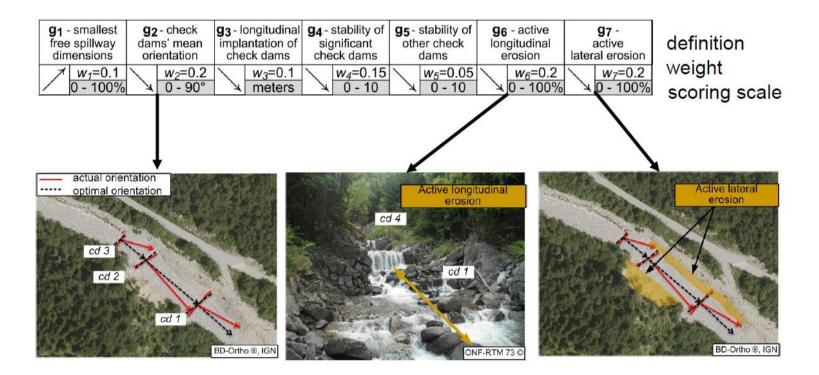






#### Identification of relevant criteria

#### 2. Effectiveness criteria $g_i$ to be taken into account







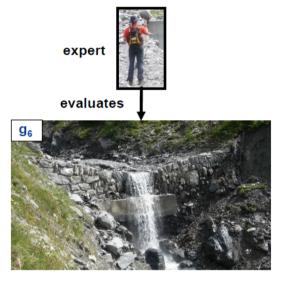




#### Considering information imperfection to assess criteria

#### Expert assessment of structural effectiveness

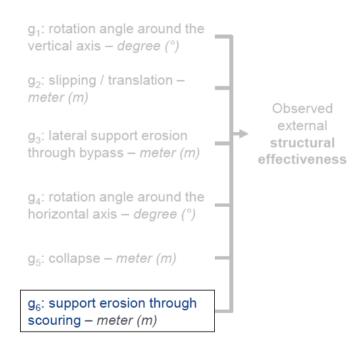
is actually based on imperfect information to evaluate each criterion



"<u>I'm sure</u> the scouring depth is lower than 4 m and higher than 2 m.

<u>I'm 30% sure</u> it is lower than 3.5 m and higher than 2.5 m."

Imprecise and uncertain information





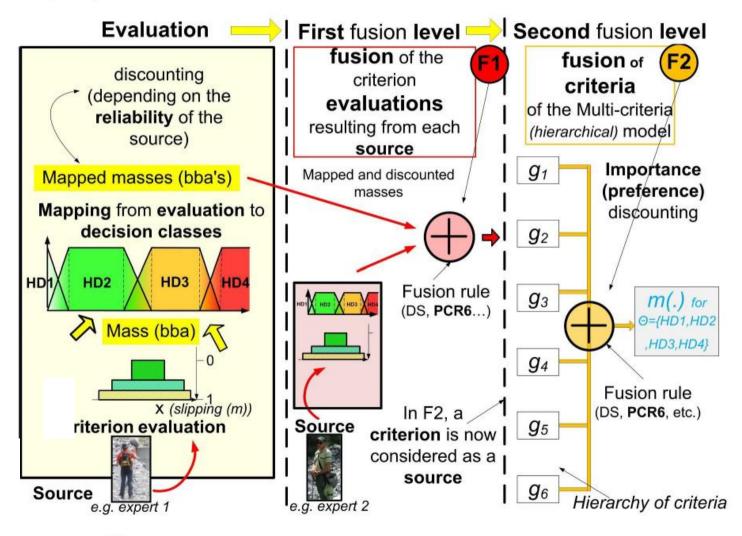






#### Imperfect assessment are fused to take a decision

### Evidential Reasoning for Multi-Criteria Decision Analysis (Tacnet, 2009)



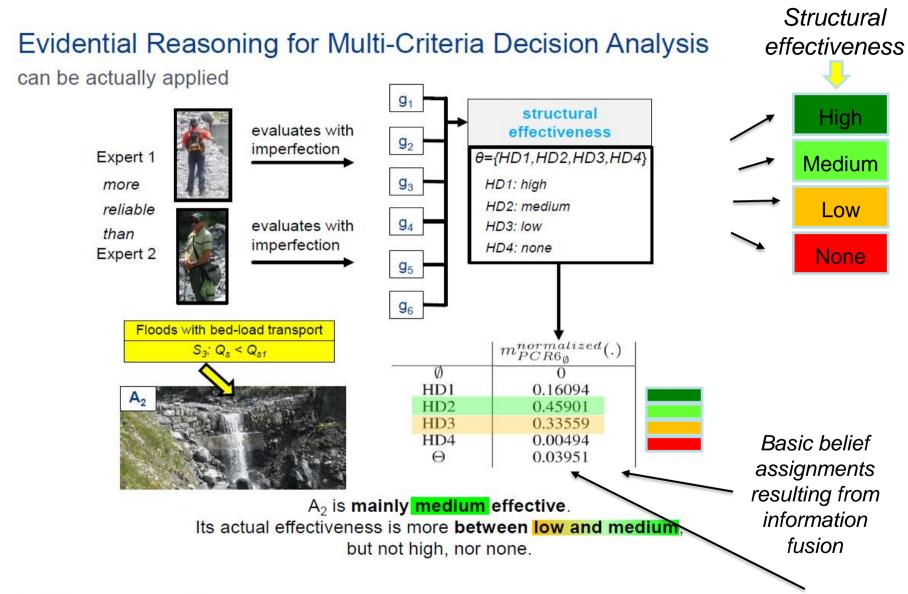








#### Imperfect assessment are fused to take a decision











# Key home messages









- 1) Uncertainty is not the only kind of information imperfection: several frameworks
- 2) Risk management requires taking decisions based on imperfect, heterogeneous knowledge and more or less reliable sources: some models exist to assess risk, to trace reasoning process and to help decision-making
- 3) Considering multicriteria decision-aiding methods, some paradoxes remain: simple methods may have drawbacks but are understandable. Powerful methods are difficult to explain and understand, they become black-boxes...
- 4) Considering information imperfection is possible but using it for decision-making remains tricky since nobody (incl. a decision-maker) likes « uncertainties »

On-going applications relates to protection and strategies' effectiveness assessment and preventive maintenance of infrastructures, protection works

## **BONUS**

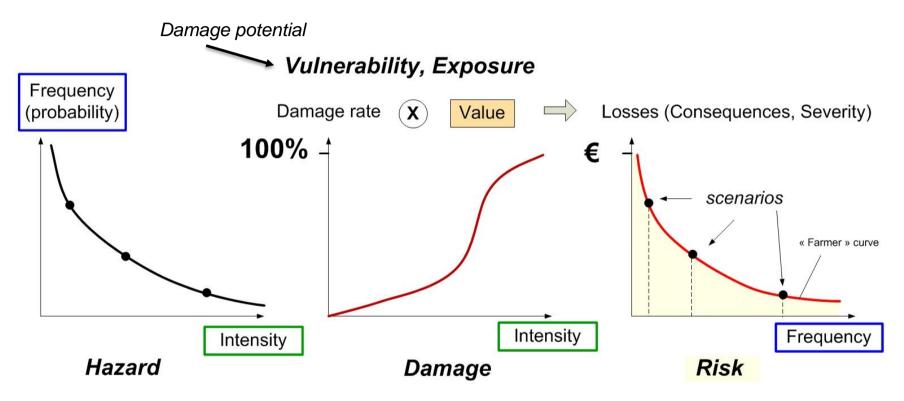








### Risk components



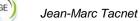
Source Tacnet et al., 2020 - Naiad project











### How to decide with belief functions? Several strategies (e.g.)

#### Maximum of belief (pessimistic/cautious)

$$m(\cdot) \to Bel(\cdot)$$
 and  $\delta = \hat{\theta} = \arg \max_{\theta_i \in \Theta} Bel(\theta_i)$ 

#### Maximum of plausibility (optimistic)

$$m(\cdot) \to Pl(\cdot)$$
 and  $\delta = \hat{\theta} = \arg \max_{\theta_i \in \Theta} Pl(\theta_i)$ 

**Compromise** with **transformation** into a **probability** (e.g. BetP, links with probabilities)

$$m(\cdot) \to P(\cdot)$$
 and  $\delta = \hat{\theta} = \arg \max_{\theta_i \in \Theta} P(\theta_i)$ 









# Soft ELECTRE TRI (SET) method

for sorting alternatives into categories based on multi-criteria analysis

Introduction of BF Theory in ... ELECTRE = ELimination Et Choix Traduisant la REalité [Roy 1968]

ELECTRE (1968) - ELECTRE TRI (1992) - Soft ELECTRE TRI [Dezert-Tacnet 2012]





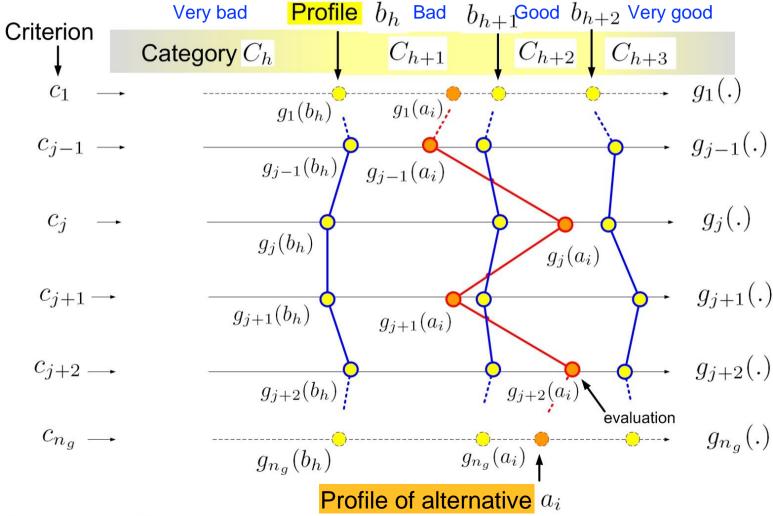




### Sorting alternatives in categories

For each criteria, we preset categories by some profile bounds

Which category does  $a_i$  belong to?  $a_i > b_h$ ?





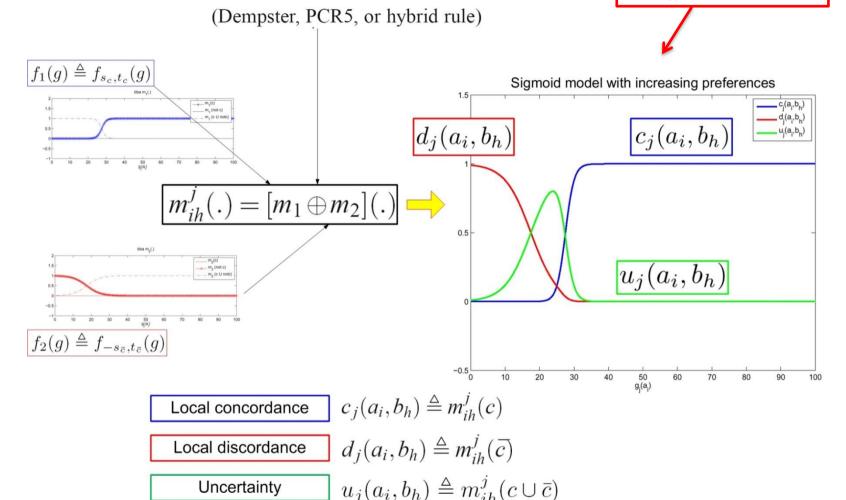






# From partial concordances and discordance indices to sigmoidal based bba's

More consistent representation



c means that the alternative  $a_i$  is concordant with the assertion " $a_i$  is at least as good as profile  $b_h$ "  $\bar{c}$  means that the alternative  $a_i$  is opposed (discordant) to this assertion

 $c_i(a_i, b_h) + d_i(a_i, b_h) + u_i(a_i, b_h) = 1$ 









with

### Soft ELECTRE TRI - An application to storm risk assessment

#### Physical parameters related to storm hazard are transformed in criteria

PConv is the 3-h accumulated precipitation

**LI** is the lifted index which characterizes the **instability** of the atmosphere

CAPE is the convective available potential energy

DivB is the low-level wind divergence if convective

clouds in the cell

**DivS** is the **wind divergence above** the top of the convective **clouds** 

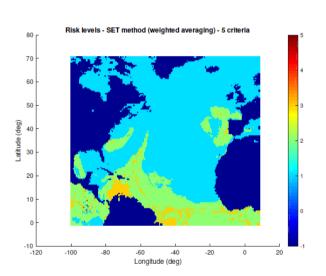


Figure 9: Storm risk levels based on SET (averaging rule).

Criteria	Units	Preference ordering	Importance weight
$G_1 = PConv$	$kg/m^2$	increasing	very high
$G_2 \models LI$	$^{\circ}K$	decreasing	very high
$G_3 = \text{CAPE}$	J/kg	increasing	high
$G_4 = \text{DivB}$	$s^{-1}$	decreasing	low
$G_5 = \text{DivS}$	$s^{-1}$	increasing	low

Table I: Criteria used for SET method.

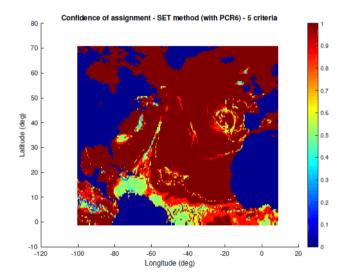


Figure 12: Confidence in decision (SET with PCR6 rule).

Rate of good lightning prediction is 95%; rate of false alarms (false predictions) is 29%.











#### Many decisions involving several actors at different steps have to be taken to assess and manage risks

**PROTECTION** 



**Decisions** for nonstructural mitigation measures

**Decisions** for choice of protection works design and maintenance strategies

Decisions for (railroad) infrastructure management

PREVENTION



2009 (L. Bernard/National Park of Mercantour )



Debris-flows

Torrent St Antoine - Modane - Savoie - 1987( M. Meunier - Cemagref)

What are the hazard, risk levels?

Land-use planning: where should urbanisation be prohibited, regulated or fully allowed?



Deposition zone



Which protection is needed? Is it effective?



EVENT MANAGEMENT





Should we close, re-open, monitor this road?

(Tacnet et al., 2014)

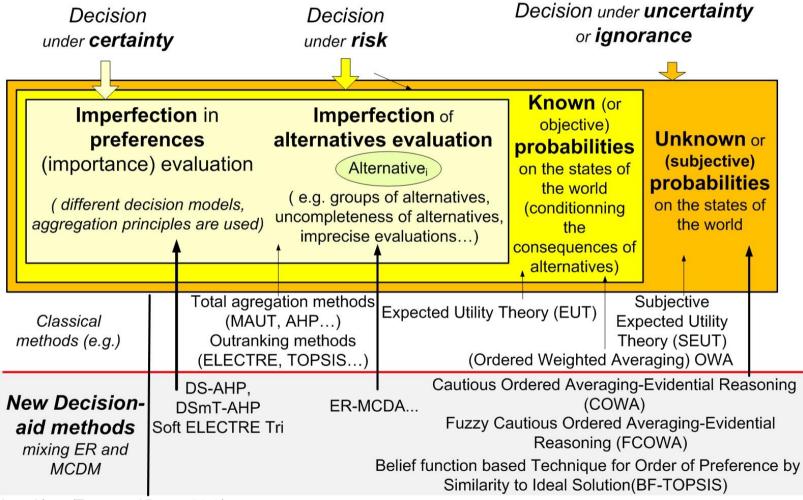








Several (other) methods exist to decide under imperfect information contexts mixing uncertainty theories and multicriteria decision-making methods (e.g.) ...



Adapted from (Tacnet and Dezert, 2012)









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# **Total aggregation methods** (based on preference transitivity assumption): AHP, MAUT...

Multicriteria decisions typology: to choose, sort, rank... alternatives

